

**1. Sequence**

5 seconds

20 points

You are given a sequence  $a_1, a_2, \dots, a_N$ . The value of each item is the index of the item to which you can move from that item.

Write a program to determine whether it is possible, starting from the first item, to return to the same item.

**Input.** On the first line of the text file `JADA.SIS` is integer  $N$  ( $1 \leq N \leq 100,000$ ) — the number of items in the sequence. On the second line of the file are  $N$  integers, separated by spaces — the items  $a_1, a_2, \dots, a_N$ .

**Output.** The first line of the text file `JADA.VAL` should contain the word `JAH`, if it is possible to return to the first item, or the word `EI`, if this is not possible. If it is possible to return, the second line of the file should contain the minimal number of steps required to do so.

**Example.**

<code>JADA.SIS</code>	<code>JADA.VAL</code>
4	JAH
2 3 1 1	3

**Remark.** The moves are as follows:  $a_1 = 2 \rightarrow a_2 = 3 \rightarrow a_3 = 1 \rightarrow a_1$ , total 3 steps.

**Example.**

<code>JADA.SIS</code>	<code>JADA.VAL</code>
4	EI
2 3 2 1	

**Remark.** The moves are as follows:  $a_1 = 2 \rightarrow a_2 = 3 \rightarrow a_3 = 2 \rightarrow a_2 = 3 \rightarrow a_3 = 2 \rightarrow \dots$  and so on forever.

**Grading.** Points for negative test cases are awarded only to programs that solve correctly at least one positive test case.

**2. Relatives**

5 seconds

40 points

There are  $N$  guests invited to a party, and some of them are known to be relatives.

Of course, the relationship of being a relative is symmetric (that is, if  $A$  is a relative of  $B$  then  $B$  is a relative of  $A$ ) and transitive (that is, if  $A$  is a relative of  $B$  and  $B$  is a relative of  $C$  then  $A$  is a relative of  $C$ ).

Write a program to find a group of maximal possible size in which no two persons are relatives of each other.

**Input.** On the first line of the text file `SUG.SIS` are two integers,  $N$  and  $K$  ( $1 \leq N \leq 100$ ,  $0 \leq K \leq N(N-1)/2$ ), separated by a space, where  $N$  is the number of guests and  $K$  is the number of explicitly given facts about relationships between them. All guests are labelled  $1 \dots N$ . Each of the following  $K$  lines contain two integers,  $A_i$  and  $B_i$  ( $1 \leq A_i \leq N$ ,  $1 \leq B_i \leq N$ ), separated by a space, meaning that the guests  $A_i$  and  $B_i$  are relatives.

**Output.** The first line of the text file `SUG.VAL` should contain an integer  $M$ , the maximal size of a group of non-relatives. The second line should contain  $M$  integers, separated by spaces — labels of the guests in the group. If there are multiple groups with the maximal size, any one of them could be listed.

**Example.**

<code>SUG.SIS</code>	<code>SUG.VAL</code>
5 3	2
1 2	1 3
3 4	
5 1	

**3. The crontab file**

open tests

40 points

In a computer system, it is often necessary to perform some actions according to a given schedule. In Unix-like operating systems, this service is offered by a program called `crond` (Greek *chronos* 'time' and *dæmon* 'spirit') that reads the schedule from a file called `crontab`.

Each line of the `crontab` file consists of six fields separated from each other by spaces or tabs. Five first fields (which may not contain spaces or tabs) describe the schedule of performing an action and the last one contains the command to be executed for performing this action.

The fields that describe the schedule are: minutes (0...59), hours (0...23), dates (1...31), months (1...12), and weekdays (0...6, where 0 = Sunday, 1 = Monday, ..., 6 = Saturday). Each field may contain a star (\*), which means all valid values, or a comma-separated list. In a list, each item may be either a valid value or two values separated by a dash (-), meaning all valid values from the first value to the second one (the boundary values themselves included).

Generally, the command is executed at times satisfying all the given conditions. For example, if the minutes field contains 0,30 and hours field contains 12-14, the command is executed at 12:00, 12:30, 13:00, 13:30, 14:00, and 14:30. The date and weekday fields are an exception. If both of these fields contain a non-star, the command is executed at times meeting either of the conditions. For example, if the date field contains 10,20 and the weekday field contains 5, the command is executed on the 10th and 20th day of month (regardless of the weekday) and every Friday (regardless of the date).

You are given a list of commands and the times when they should be executed. The task is to create a `crontab` file scheduling all the given commands for execution at specified times with as few lines as possible. If several commands are to be executed at the same time, they are really executed in the order of their entries in the `crontab` file. Your reconstructed `crontab` should preserve that order.

**Input.** Each line of the text file `CRON.SIS` contains three space-separated fields: the date in the form DD.MM.YYYY, the time in the form HH:MM, and the command to be executed on this date at this time. The file is complete: it lists all actions to be performed from the moment specified on the first line to the moment specified on the last line. The lines in the file are given in chronological order.

**Output.** The text file `CRON.VAL` should contain the `crontab` to make `crond` to execute exactly the desired commands in the given timeframe. What would happen before the first or after the last moment specified in the input file does not matter.

<b>Example.</b>	<code>CRON.SIS</code>	<code>CRON.VAL</code>
	20.10.2003 12:00 test	0 12-14,17 * * * test
	20.10.2003 13:00 test	
	20.10.2003 14:00 test	
	20.10.2003 17:00 test	
	21.10.2003 12:00 test	

**Remark.** The `crontab` given in the output file executes the command `test` every day at 12:00, 13:00, 14:00, and 17:00. Thus the list of actions performed from 12:00 on 20.10.2003 to 12:00 on 21.10.2003 matches the list given in the input file. Therefore, the given `crontab` meets the requirements, even though the command `test` is also executed before 20.10.2003 and after 12:00 on 21.10.2003, in particular at 13:00, 14:00, and 17:00 on 21.10.2003.

**Grading.** In this task, you are given 10 specific input files named `cron01.sis` to `cron10.sis` and you should, as your solution, submit the corresponding output files named `cron01.val` to `cron10.val`. It is not necessary to submit a program. Every correct output file receives points inversely proportional to the ratio between the number of lines in this file and the best solution submitted (that is, a file with twice the number of lines receives half the points).